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Sentiment-Aware Volatility Forecasting

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Abstract

Recent advances in the integration of deep recurrent neural . * . orks and statistical inferences have paved new avenues for joint modeling of moments or rander variables, which is highly useful for signal processing, time series analysis, and financial recasting. However, introducing explicit knowledge as exogenous variables has rece. ad litt¹, attention. In this paper, we propose a novel model termed sentiment-aware volating (SAVING), which incorporates market sentiment for stock return fluctuation prediction. Our framework provides an ensemble of symbolic and sub-symbolic AI approac. s, that is, including grounded knowledge into a connectionist neural network. The model aims at producing a more accurate estimation of temporal variances of asset returns by better c ptr ang the bi-directional interaction between movements of asset price and market sentiment. The interaction is modeled using Variational Bayes via the data generation and inference circ. tions. We benchmark our model with 9 other popular ones in terms of the likelihood of forec. ts given the observed sequence. Experimental results suggest that our model not only ou performs pure statistical models, e.g., GARCH and its variants, Gaussian-process volatility model, but also outperforms the state-of-the-art autoregressive deep neural nets architectures, which as the variational recurrent neural network and the neural stochastic volatility model.

networks; Financial text mini .g.



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1. Introduction

Moments of asset returns carry important information in financial decisio. moking. For example, the expected returns are calculated as the mean of return series, and volatility is measured by a covariance matrix over assets. For simplicity, the classic approach to polyfolio management [1] (also called the mean-variance analysis framework) ignores higher moments and only considers the first two orders of moments of asset returns to diversity the investment. Under this framework, the constrained utility maximization problem is for matrix or a quadratic opti-

mization problem to maximize expected return and minimize the portfolio isk at the same time. Modern ways of derivatives pricing also heavily rely on the concepts of as set price and volatility, such as in the Black-Scholes model [2, 3]. Among thes concepts, volatility is believed to be comparatively more difficult to approximate due to its complete edited temporal dependency structure.

Traditional econometric models, such as the generalized au. regressive conditional heteroscedasticity (GARCH) group [4], formulate the time-varying volatility as a deterministic linear function

- of the past variable observations and its lagged items. However innancial data are characterized by chaotic behaviors and a poor signal-to-noise ratio. Observations suggest that linear modeling of volatility tends to be unstable and overfits to lear randomness. Another method to model volatility in a deterministic generative manner is using a latent stochastic process as prior [5], hence called "stochastic volatility".
- Recently, using deep recurrent neural network (RNN) for sequential modeling has become popular. Successful applications of deep RI have been reported on hand-writing recognition and speech synthesis. Compared to previous been reported on hand-writing recognition driven approach to implicitly learn the an analysis of function. Therefore, it is claimed to have extra expressive power to capture the non-in par variation of volatility [6, 7]. The variational
- RNN (VRNN) is a hybrid of variational autoencoder and RNN which can be naturally used for joint modeling of a stochastic variable with its mean and variance [7], where the conditional distribution of the variable is gen, and from a Gaussian process determined by latent variable states. The neural stochastic vol. tility note that (NSVM) further extends VRNN with autoregressive architecture for the hidden state, bi directional architecture for variable encoding, and stochastic sampling techniques [8] to for the form of the variable form volatility model.

Both VRNN [7] and SVM [8, take information only from the past observations. In the context of predicting ex ected stock returns and its volatility, the input information will be the historical prices and return sequences. One major concern of directly applying VRNN or NSVM is that, the role of in esto's or market participants is absent in their model settings [9]. In the

- real world, unfortunated asset price fluctuations can be driven by events [10] and market sentiment [11, 12], or ven irrate nal or collective actions that happens for no obvious reason. Implied volatility is thus very sensitive to the news and social media response [13, 14, 15, 16]. Omitting exogenous variable, can hus be a defect in the attempt of constructing such a forecasting system. To addreps this issue, we propose to extend VRNN volatility modeling by integrating senti-
- ⁴⁵ Jc nr-modeling of asset returns and market sentiment in a variational recurrent neural amework, instead of simple concatenation and normalization of the two heterogeneous

sources of knowledge.

2. Providing an interface for deep neural models to acquire explainable sertimer information from knowledge bases, bridging the gap of knowledge-based systems and pure machine learning systems.

Experimental results show that the SAVING model can achieve a' impliced performance on the task of volatility forecasting compared with the state-of-the-arce or arent neural models. In fact, on our dataset, the difference between the previously proper direct. Some neural models and the deterministic linear models are not significant, though they all some to be better than naïve architectures with no effort made on adapting data feature. We' elieve the room for improvement with an autoregressive model is limited and atticute use merit of the SAVING model to the fact that it effectively incorporates market sentir ent for the predictive process.

The remainder of the article is organized as follows: Section 2 pr vides background for the compared methods, including econometric models and the ViNN model; Section 3 shows how the polarity score for each message is computed with the help of a knowledge base and the sentiment aggregation/quantization process to form a disciple optimistic section 4 describes the variable operations in the SAVING model; ext, Section 5 reports and discusses experimental results; finally, Section 6 summarizes charge research and Section 7 concludes the article with future work.

65 2. Background

In this section we provide some backgrou. d about our baselines, including the GARCH model, the state-of-the-art VRNN model, multi-ariants such as NSVM.

2.1. Linear Volatility Modeling

Time-varying variance is a cor mon phenomenon for financial time series, that is, strong fluctuations are clustered in certain time periods. Constant-variance models, e.g., the Autoregressive Moving Average (ARMA) model are not suitable for modeling such time series. Consequently, deterministic linear modeling of colative ity is proposed. The GARCH model [4] is one of the most recognized among them, which models a time series x_t by a Gaussian process and its time-varying variance $\sigma_{x,t}^2$, as in Eq. (1) and Eq. (2):

$$\sigma_{x,t}^2 = \alpha_0 + \sum_{i=1}^p \alpha_i x_{t-i}^2 + \sum_{i=1}^q \beta_j \sigma_{t-j}^2, \tag{1}$$

$$x_t \sim \mathcal{N}(0, \sigma_{x_t}^2). \tag{2}$$

where p is the moving a grage order and q is the autoregressive order. Together, they characterize the number of parameters a GARCH model would have. Since each variable x_t is sampled from a local Gau sian distribution with zero mean, the residuals will always follow $\epsilon_t^2 \equiv x_t^2$. In this context, Eq. (1) in the facto an ARMA model of $\sigma_{x,t}^2$.

Variants of the GARCH model include ARCH [17], where autoregressive coefficients β are set to z ro; EG/ RCH [18], where $\log(\sigma_{x,t}^2)$ is used instead of $\sigma_{x,t}^2$ and a bias is imposed on x_t to address asymmetric volatility; GJR-GARCH [19], where asymmetric volatility is expressed by adding $\delta x_{t-1}^2 I_{t-1}$ to the right side of Eq. (1) where $I_{t-1} = 0$ if $x_{t-1} \ge 0$ and $I_{t-1} = 1$ if $x_{t-1} < 0$.

We reconsider random variable x_t in Eq. (1) by decomposing it to a det ... inistic timedependent $\sigma_{x,t}$ and a latent standard Gaussian process $z_t \sim \mathcal{N}(0, 1)$:

$$x_t = \sigma_{x,t} \cdot z_t. \tag{3}$$

This decomposition inverses the idea of the reparameterization trick [2C₁ to j ... duce z_t , though the stochastic item z_t is eliminated from the GARCH model by taking quare. However, in stochastic volatility models z_t can be a separate item where x_t is dramed subsequently, a new set of parameters γ may be introduced. In real-world data, though, r manter α and β may have more complicated form. Therefore, a general form volatility model can be costracted as Eq. (4),

$$\sigma_{x,t}^2 = f_{[\boldsymbol{\alpha},\boldsymbol{\beta},\boldsymbol{\gamma}]}(\sigma_{x,
(4)$$

where $\sigma_{x,<t}^2$ can be further eliminated [8]. In this case, we volumity is specified from this process:

- 1. generation of autoregressive latent process $z_{\leq t}$;
 - 2. generation of past observations $x_{<t} = g(z_{<t})$;
 - 3. generation of $\sigma_{x,t}^2$.

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Note that the analytical solution of function f in $\sum_{n=1}^{\infty} (A)$ may not be easy to specify as the number of parameters grows large. Fortunately, recent as a^{n} ces in deep learning provide us a new way to parameterize f.

2.2. VRNN for Sequence Modeling

Suppose we have a sequence of observations $x = (x_1, x_2, ..., x_t)$, a basic RNN learns the parameters θ of a neural network f and keeps updating its hidden state h_t as in Eq. (5):

$$h_t = f_\theta(x_t, h_{t-1}). \tag{5}$$

The neural network f_{θ} may consist of any neuron structures, such as the long short-term memory (LSTM) [21] and gated recurrent on unit (GRU) [22]. In a standard RNN [23], the computation follows Eq. (6) and Eq. (7)

$$x_t - W^{ho}h_{t-1} + b^o (6)$$

$$h_t = \tanh(W^{hh}h_{t-1} + W^{hx}x_t + b^h)$$
(7)

where W^{**} are transition patrices spanning timesteps and b^* are biases that define θ . A high-level illustration of the computation process is provided in Figure 1.



Figu. : A basic RNN model that outputs x_t (dashed arrow) and keep updating its hidden state h_{t-1} (solid arrow).

The RNN computation in Eq. (5) implicitly models a regressor for x_t base $\neg \neg$ all past observations $x_{< t}$ through substituting $h_{< t}$. However, $\sigma_{x,t}$ does not appear. A neve volatility forecasting technique to induce $\sigma_{x,t}$ is to estimate σ_t^2 with σ_{t-1}^2 , that is to write $\neg \cdot$ (8):

$$\sigma_{x,t}^2 = \operatorname{Var}(x_{< t}) = \frac{1}{(t-1)^2} \sum_{i=1}^{t-1} \sum_{j>i}^{t-1} (x_i - x_j)^2.$$
(8)

However, the expressive power of Eq. (8) is restricted. It will be cl_{ℓ} are if we look at the lagged-form of Eq. (8):

$$\sigma_{x,t}^2 = \left[1 + \left(\frac{t-2}{t-1}\right)^2\right]\sigma_{x,t-2}^2 + \frac{\sum_{i=1}^{t-1} (x_{t-1} - \ldots)^2}{(t-1)^2}.$$
(9)

The autoregressive coefficients are not *learned* as in deterministic livear volatility models, but will only be a fixed function of t. For this reason, we argue that the standard RNN does not suffice complicated volatility modeling. Or, in other words, the standard RNN cannot generate sequences with certain types of time-varying volatility

To solve this problem, a VRNN integrates the archivecture of a variational autoencoder (VAE) [20]. Using the probabilistic parameterization of use joint distribution of x and the latent variables z, the hidden state h as in RNNs is by $a_{e_{x}}$ on characterized by mean and variance information in a Gaussian case. For this reason, we use write the generative model as Eq. (10):

$$p(\boldsymbol{x}|\boldsymbol{z}) \sim \gamma(h^{\mu}(\boldsymbol{x}), h^{\sigma}(\boldsymbol{z}))$$
(10)

where volatility item $\sigma_{x,t}$ is embodied in the hic ¹en state h.

We expand Eq. (10) across time steps.

$$p(x_t|z_{\leq t}, x_{\leq t}) \sim \mathcal{N}(h^{\mu,\sigma}(g_\tau(z_t), h_{t-1}))$$

$$(11)$$

$$p(z_t|z_{t}, x_{< t}) \quad \mathcal{N}(h^{\mu, \sigma}(g_v(x_t), h_{t-1})) \tag{12}$$

where g_{τ} and g_{υ} are neural net vorks w proximate the non-linear functions. The parameterization of VRNN is therefore:

$$p(z_{i}, z_{\leq t}) = \prod_{i=1}^{t} p(x_{i}|z_{\leq i}, x_{< i}) p(z_{i}|z_{< i}, x_{< i}).$$
(13)

where $p(x_{\leq t}, z_{\leq t})$ is join probability of all the observations. Like in Eq. (5), hidden state of a VRNN is updated and "g ineration of z_t and x_t (see Eq. (11) and Eq. (12)):

$$h_t = f_\theta(g_v(x_t), g_\tau(z_t), h_{t-1}).$$
(14)

3. Sentime a time Series

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Our goal being 's integrate sentiment signals from social message streams into a volatility model, 's e first transform the streams into a sentiment time series. In this section, we discuss how a sentiment variable s_t is defined. We represent the sentiment information for a specific asset A as a qual truple that is, to calculate sentiment polarity and intensity for each relevant message an 'garegate them in a discrete-time axis. We have:

$$s_t(A) = (s_t^I(+), s_t^I(-), s_t^V(+), s_t^V(-)).$$
(15)
5

where $s_t^I(+)$, e.g., is the average intensity for all the positive messages, and $\frac{V}{t}(-)$ the count of negative messages regarding A. One can obtain the polarity score of a ness ge by many techniques, e.g., training a neural network for sentiment analysis. In the SAVIN would however, we employ a knowledge-based method to embrace high interpretability and brage the gap between connectionist models and many other disciplines, such as cognitive inguistics and commonsense reasoning [24, 25].



Figure 2: Polarity computing via reasoning thro h a typed ependency tree.

3.1. Polarity Computing

We compute the polarity score of each message usi. 3 augmented sentic computing [26]. This approach relies on a group of linguistic rul, s to explicitly catch the long-term dependency in texts. Unlike its predecessor [27], which leveral is polarity algebra, augmented sentic computing implements modificatory functions for different pivot types. A message is first parsed into multiple relation tuples with the Stanford Upen dependency parser [28]. Later, a semantic parser will look at each uni-gram and bi-gimmand attempt to acquire the polarity score from a concept-level sentiment knowledge base. We can ploy the latest version of SenticNet [29], which contains 100,000 natural language compute.

- Figure 2 provides an example of how polarity scores of concepts are propagated along the dependency structure. Two concepts goed own and stupid are identified with polarity score of -0.07 and -0.93 respectively. The polarity of stupid is passed through a nominal subject relation so that the multi-work expression this is stupid inherits the score of -0.93. Similarly, the other high level relative re
- feeling_(that) AP. would_go_down triggers an amplified intensity of $-\sqrt{|-0.07|} = -0.27$. Note that the two struct. we are linked by an adversative but-conjunction, the overall polarity is thus calculate i.e. $\sqrt{|[(-0.27) + (-0.93)]/2|} = +0.78$ and passed to the root of the sentence. The comp ting process is backed-up with a multi-layered perceptron (MLP) network to solve zero-shot problem: if no concept is acquired from the knowledge base, the polarity is derived from sup rvis d learning. Finally, if a message consists of multiple sentences, the overall polarity score w." b an everage of each sentence polarity score.

Messag s arrive continuously with a timestamp T_i . Discrete-time operations, e.g., trading, will entail a ily sent ment quantization. Taking market closure into consideration, we aggregate market so time... from the previous trading day to one hour before the closing time. Algorithm 1 elabor tes the process for sentiment time series construction.

Only ... ingful part-of-speech tag pairs, such as ADJ+NOUN, VERB+NOUN, and VERB+ADV are considered and lemma '~ d.

Alg	gorithm 1: Constructing sentiment time series.
Ι	Data: message stream of a specific asset $\{m_i, T_i\}$
F	Result: sentiment time series $s_t(A)$
1 f	or $i = 1, 2,$ do
2	if $T_i < t$ then
3	$C(m_i) \leftarrow \text{parse concepts from } m_i;$
4	if $C(m_i) \bigcup KB \neq \emptyset$ then
5	$s(m_i) \leftarrow$ augmented sentic computing m_i ;
6	else
7	$s(m_i) \leftarrow MLP(m_i, \Theta);$
8	end
9	if $s(m_i) > 0$ then
10	$ s_t^I(+) \leftarrow \frac{n-1}{n} s_t^I(+) + \frac{1}{n} s(m_i);$
11	$s_t^V(+) \leftarrow s_t^V(+) + 1;$
12	else if $s(m_i) < 0$ then
13	$ s_t^I(-) \leftarrow \frac{n-1}{n} s_t^I(-) + \frac{1}{n} s(m_i);$
14	$s_t^V(-) \leftarrow s_t^V(-) + 1;$
15	$n \leftarrow n+1;$
16	else
17	$t \leftarrow t+1; \ [s_t(A), n] \leftarrow 0;$
18	end
19 e	nd
20 r	eturn $s_t(A) \leftarrow (s_t^I(+), s_t^I(-), s_t^V(\neg), s_t^{-}(\neg));$

4. Sentiment-Aware Volatility F recasting

We describe the three types of variable operations (generation-recurrence-inference) in the SAVING model with the presence of centiment variable s_t (see Figure 3). To incorporate s_t , the latent variables will be shared by c_t and s_t , and the hidden state will be a concatenation of dimensions including reference of the two states and latent variables z. In this sense, we use bold notation z_t and h_t slightly different from that in VRNN. In VRNN, the bold notations z_t and h_t denote vector representations for each time period t, whereas in the SAVING model, for example, z denotes the full history of $z_t, z_{t-1}, z_{t-2}, \ldots$.

Our goal is to 'earn \sim o complicated dynamics of variable interactions with an implicit function \mathcal{F} of Eq. (1 ℓ):

$$\mathcal{F}(\sigma_t, x_{< t}, s_{< t}, \boldsymbol{z}_{\le t}) = 0.$$
(16)

With the sha cd latent variables and their autoregressive nature, namely p(z_t|z_{<t}) ~ N(µ_{z,<t}, σ²_{z,<t}), two symmetric caus. I chains s_{t-1} → z_t → x_t and x_{t-1} → z_t → s_t are built up to model the bi-directional interaction between movements of asset price and market sentiment. Although this intraction has been justified by Granger causality test from both sides [30, 14, 15], the SAV-ING n odel is the first deep RNN architecture to elegantly capture this feature to the best of our knowled_b ^(cc). Figure 4).



Figure 3: Graphical illustration of the SAVING model: 3(a) joint generating 'roce's for sset return and sentiment from hidden state and latent variables; 3(b) updating hidden state of neurons; 3(c) "increncir's posterior distribution of latent variables using time-lagged items. The hidden variables are denoted by dia. "nds and observable variables by circles."



Figure 4: The full architecture c the SAVIN, model expanding on the time arrow. Generation operations are denoted by dashed arrows; recurrence c era, ns are denoted by dotted arrows; inference operations are denoted by solid arrows.

4.1. Generation

The major difference t^{t} ween the SAVING model and the VRNN [7] is that for both return and sentiment vertiables, the conditional distribution of z_t is no longer an autoregressive Gaussian distribution, but using interpretation the past input observations. For instance, generation of x_t involves the arguments:

$$p(x_t | x_{< t}, \boldsymbol{z}_t) \sim \mathcal{N}(\mu_{x,t}, \sigma_{x,t}^2), \tag{17}$$

where
$$[\mu_{x,t}, \sigma_{x,t}] = \phi_x(\varphi^x(x_{t-1}), \varphi^z(\boldsymbol{z}_t), \boldsymbol{h}_{t-1}),$$
 (18)

 $\mu_{x,t}$ and $\gamma_{x,t}$ on the parameters of the Gaussian distribution where x_t is sampled, φ^x and φ^z are $\gamma_{x,t}$ in the two states that extract information from x_{t-1} and z_t . Decoder ϕ_x maps the dimension back $\gamma_t \dim(\mu_x + \sigma_x)$.

Similarly, s_t is synchronized with z_t , denoting the sentiment accumulated '... veen the current and the previous market closing time:

$$p(s_t|s_{< t}, \boldsymbol{z}_t) \sim \mathcal{N}(\mu_{s,t}, \sigma_{s,t}^2), \tag{19}$$

where
$$[\mu_{s,t}, \sigma_{s,t}] = \phi_s(\varphi^s(s_{t-1}), \varphi^z(\boldsymbol{z}_t), \boldsymbol{h}_{t-1})$$
 (20)

 $\mu_{s,t}$ and $\sigma_{s,t}$ denote the parameters of the Gaussian distribution where \cdot is sampled, φ^s is a neural network that extracts information from s_{t-1} and ϕ_s is a dec der. To initialize the generation process, we assume the first pair of observation (x_t, s_t) is drawn from a standard Gaussian distribution.

4.2. Recurrence

The recurrent process updates the hidden state. In the \sqrt{VN} model, h_t is a concatenation of three heterogeneous memories for the latent variables, rec rn series and sentiment series respectively. Since z_t already contains joint information, its up at is independent from other parts of the model:

$$\boldsymbol{h}_t = [h_t^z, \boldsymbol{h}_t^{x,s}] \tag{21}$$

$$h_t^z = f_\theta(\varphi^z(\ h_{t-1}^z), h_{t-1}^z).$$
(22)

However, observed x_t and s_t are not integrated in the generation phase. Consequently, the hidden state will be shared by return and sentiment. For variables to facilitate forecasting through the completeness of z_t :

$$\boldsymbol{h}_{t}^{x,s} = f_{\theta}(\boldsymbol{\varphi}^{x}(x_{t}), \boldsymbol{\varphi}^{s}(s_{t}), \boldsymbol{h}_{t-1}^{x,s}).$$
(23)

where f_{θ} is the neural network to join the new observations and the previous model (see Eq. (5)).

4.3. Inference

After the hidden state is ur lated by the latest x_t and s_t , the joint distribution of observable variables will be used to inferror all distribution of z_{t+1} . Variational inference [31, 20] is employed to stochastically optime an approximation $q(z_t|x_t, s_t)$ for the posterior $p(z_t|x_{< t}, s_{< t})$, because of the difficulties real calculating the joint marginal distribution. According to Bayes' theorem, the conditional probability distribution of z_t is

$$p(\mathbf{z}_t | x_{< t}, s_{< t}) = \frac{p(x_{< t}, s_{< t} | \mathbf{z}) p(\mathbf{z})}{p(x_{< t}, s_{< t})},$$
(24)

where the integral $p(z_{<t}, z_t) = \int p(x_{<t}, s_{<t} | z) p(z) dz$ is computationally intractable since z is unknown. There, we learn parameters $\mu_{z,t}$ and $\sigma_{z,t}$, such that

$$q(\boldsymbol{z}_t | \boldsymbol{x}_t, \boldsymbol{s}_t) \sim \mathcal{N}(\boldsymbol{\mu}_{\boldsymbol{z}, t}, \sigma_{\boldsymbol{z}, t}^2),$$
(25)

where
$$[\mu_{z,t}, \sigma_{z,t}] = \psi(\varphi^z(\boldsymbol{z}_{t-1}), \varphi^{x,s}(\boldsymbol{x}, \boldsymbol{s}), \boldsymbol{h}_{t-1}).$$
 (26)

Encodyr ψ map the dimension to dim $(\mu_z + \sigma_z)$.

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4.4. Learning

Parameters of the encoding and decoding neural networks, i.e. ϕ_x , ϕ_s , ar ψ : co-trained using stochastic gradient descent. Recall that our objective is to minimize the K. ¹back-Leibler divergence between $q(z_t|x_t, s_t)$ and $p(z_t|x_{< t}, s_{< t})$:

$$KL(q_t||p_t) = -\sum_{i=1}^t p(x_{\le i}, s_{\le i}) \ln \frac{q(\mathbf{z}_i|x_i, s_i)}{p(x_{\le i}, s_{\le i}, \mathbf{z}_i)}$$
(27)

Since the integral of joint distribution $\int p(x_{\leq i}, s_{\leq i}) dx ds$ is fixed vith a scies of observations, minimizing the Kullback-Leibler divergence is equivalent to maximizing, the Evidence Lower Bound (ELBO). After independent factorization of the gene ation is d inference processes by substituting conditioning variables with time-lagged items, that is function can be written as a negative ELBO [32]:

$$\ell(q) = \sum_{i=1}^{t} [KL(q_i||p_i) - \ln p(c \cdot s_i|_{\bullet} \cdot c_i, z_i)].$$
(28)

Then we apply gradient descent until convergence 10.

$$\begin{cases} \phi_x &\leftarrow \phi_x & \rho \circ \widehat{\langle \cdot \rangle} / \partial \phi_x \\ \phi_s &\leftarrow \phi_s - \rho \cdot \ell(q) / \partial \phi_s \\ \psi &\leftarrow \psi \circ \partial \iota(q) / \partial \psi \end{cases}$$
(29)

where gradients over the variational distribution q is actually intractable. However, we can eliminate q via Monte Carlo sampling [33]. We traw S samples of the latent variables z to approximate the gradient of the loss function:

$$\partial \ell = \frac{1}{F} \sum_{i=1}^{r} \ln \frac{p(x_{\leq i}, s_{\leq i}, \boldsymbol{z}_i)}{z_i | x_i, s_i)} \partial \ln q(\boldsymbol{z}_i | x_i, s_i).$$
(30)

In the SAVING model, a.' the sar ples are assumed to be Gaussian. Due to its recursive nature, the forecasting hor zon ca. ' e arbitrarily set once the learning phase is accomplished. Nevertheless, it is alway a commended to re-train the model once new observations are received. In our experiment settines, the volatility forecasting is one-step-forward. This setting also ensures that the esting is strictly out-of-sample and over-fitting is reduced to a minimum level.

160 5. Experiment

We empi cally investigate the effectiveness of the SAVING model over a range of baselines in the litera are usin, historical stock price data and social media streams.

5.1. Dr. a Preparation

A ligh-qual ty source for constructing sentiment time series is crucial to the performance of the SAV TGr. odel. We employ StockTwits², a social media platform for sharing ideas between

²htt_h /stocktwits.com/

investors, traders, and entrepreneurs. We believe that the professional platfor ... contains less noisy information compared to general-purpose venues, such as Twitter. Jue t the limited accessibility of historical data, we test the SAVING model on 10 US stocks w., relatively big market capitalization for over one year (from August 14, 2017 to August 22, 2010). In total, 82.2MB of textual data are collected, out of which a small portion is us r-labeled. Table 1 lists the stock tickers, user-labeled numbers of positive and negative m ssag s, positive/negative

ratios, and the total numbers of messages in this period.

The messages associated with one specific company are filtered by cashtags³. To align sentiment time series and return series, we cut off the messages after 3:0 P.M. for the next trading day.

This configuration allows for one hour of trading operations before mark ι closure in practice. The price series are transformed to daily log returns $x_t = \log(price_t price_{t-1})$ and normalized before feeding into the SAVING model. For both return set as and sentiment time series, the missing values are filled by the closest previous record.

5.2. Model Settings

- 180
- In our experiments, hyperparameters are set as following: the dimension of sentiment variable is set to dim $s_t = 4$ to include both intensity and variable is univariate and stock-specific, though 10 stock pairs (x_t, s_t) are concatenated for training to allow for modeling relationships of connected stocks; GRU cells are used for RNN function f_{θ} with 20% dropout and other neural not works such as ϕ_x , ϕ_s , ψ , φ^x , φ^s , and φ^z are implemented with two-layered MLPs, where each not ver has 10 neurons.

Ticker	#Pos.	#Neb	Pos./Neg. ratio	Total
AAPL	28, ⁴ , 5	·?, 040	2.37	130, 425
AGN	1, 132	592	2.42	8,622
AMZN	27,90∠	7, 029	3.97	97, 580
BABA	<i>3</i> 5, € <i>3</i> 7	4, 488	7.93	97, 253
GOOG	5 824	1, 684	3.46	23, 371
GS	3, 0. 1	1, 177	3.07	19, 142
PFE	1, 414	115	12.30	8, 946
SBUX	2, 618	1, 461	1.79	14, 873
STN P	485	112	4.33	3, 202
TS. ^	44, 398	28, 882	1.54	153, 060

Table 1: Basic data statistics. 201/-08-14 to 2018-08-22.

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The embedding times sion for hidden state is set to 15: equally partitioned for return, sentiment, and latent val. ble to create a bottleneck for the input dimension. Adagrad optimizer [36] is found to 'e exceptional for training of the SAVING model parameters, whereas when using other populit optimizers such as Adam or stochastic gradient descent the converged NLLs are much higher. The calculation of $lr = 5 \times 10^{-4}$ and save the trained model each 10 epochs for 500 epoch, in sum. The final model is empirically chosen with NLLs on the training set as the riterion. Then, this final model is used for one-step-forward forecasting only. As the

³A ⁹ ntag combines a dollar sign and some catchy word, in our context usually a stock ticker, e.g., \$AAPL.

Ticker	SAVING	GARCH [4]	EGARCH [18]	TARCH [34]	GJR [19]	GP-vol [35]	VRNN [7]	NSV' [8]	L. "M [21]	s+LSTM
AAPL	-3.2798	-3.1010	-3.1041	-3.1280	-3.1255	-3.1184	-2.9900	-2.956	-0.7271	-2.1504
AGN	-3.0387	-3.0113	-3.0113	-3.0102	-3.0129	-3.0158	-3.0296	~321	7.9030	-1.2742
AMZN	-2.9296	-2.8183	-2.8183	-2.8194	-2.8187	-2.7918	-2.8559	-2.7 61	-0.2887	-2.1488
BABA	-3.2003	-2.7253	-2.7253	-2.7228	-2.7292	-2.7229	-2.7240	-2.7 .88	-0.4521	-1.6865
GOOG	-3.2319	-3.0670	-3.0670	-3.0823	-3.0851	-3.0207	-2.9752	-7 /281	-0.4657	-2.1528
GS	-3.2609	-3.1267	-3.1267	-3.1245	-3.1333	-3.1160	-3.0121	~710	-0.4832	-0.6010
PFE	-2.8548	-3.4011	-3.4078	-3.3921	-3.4111	-3.3911	-3.1 10	-3.050.	-0.3844	-0.0159
SBUX	-2.9606	-3.1579	-3.1580	-3.1647	-3.1656	-3.1046	-?)814	- 9911	-0.5805	-1.5442
STMP	-3.1081	-2.3556	-2.3556	-2.4437	-2.4412	-2.3738	-1 3985	-2 883	-0.4343	-1.2197
TSLA	-2.7775	-2.1776	-2.3483	-2.3735	-2.3493	-2.3005	-2 `50	-^ J769	-0.2006	0.9380
Average	-3.0642	-2.8942	-2.9122	-2.9261	-2.9272	-2.8956	2.8749	-2.7617	-0.4920	-1.1856

Table 2: Performance of the SAVING model and other compared benchmarks measured by NLI · only the SAVING model and s+LSTM employ sentiment information, other models are autoregressive.

new data come in, the training set is updated and the outdated model is discarded with a re-train procedure.

The SAVING model is trained in an online fashion on Nvir a Tesla M60 GPU. The training time, in theory, will increase with the growth of hetorical data and the number of stocks considered. Empirically, convergence can be reached in minute-level for one year's data.

5.3. Compared Methods

Following the previous work [8], we adopt munimediate benchmarks from different model groups, including deterministic linear models, stoch wird volatility models, and deep recurrent neural models optionally equipped with sentiment into making.

- 1. GARCH(1,1), where only x_{t-1} and σ_{t-1}^2 are included on right hand side of Eq. (1); EGARCH(1,1), where the volatility variables are in their log form; TARCH(1,1,1) [34], where the power of σ is set to ', C'R-GARCH(1,1,1), where one lagged asymmetric shock is added.
- 2. Gaussian-process volatility mc¹el ('*i*P-vol) [35], where x_t is generated from a Gaussian process parameterized b $\mu = 0$ and σ_t^2 .
- 3. Variational neural modes 's *i* clucking VRNN [7], where the prior on latent variables is autoregressive and can be under '*i* od as a time-varying VAE, and NSVM [8], where the prior also depends on product 'servations.
- 4. LSTM [21], which consists of two layers: a recurrent layer with 10 LSTM cells, 20% dropout and re tific 1 linear unit activations (ReLU), and a dense layer of 10 neurons, summing up to 590 trainable parameters. Additionally we have s+LSTM, where sentiment and return straibles are concatenated to form an input. The naïve volatility forecasting based on sliding window of returns is implemented as with Eq. (8).

5.4. Results and Discussion

We observe some interesting facts after a quick pass through Table 1. Generally, people post far more positive recessages than negative ones on social media, at least for the scope of stocks studied. For hetspot stocks, such as AAPL and TSLA, the ratio is about 2. Less discussed stock like PF 7 has an amazingly high ratio of around 12.

It also are that frequently discussed stocks are more volatile, while stocks without much news can are have relatively stable returns. To evaluate the performance of different models we up negative log-likelihood (NLL), which assumes the predicted return and volatility form

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the ground truth distribution, and calculate the likelihood of observations. Un'... the Gaussian distribution hypothesis of x_t , NLL can also be interpreted as a mean squared ϵ .ror ℓ MSE) with a volatility-based regularization [37] (see Eq. (31)):

$$NLL = -\sum_{i=1}^{t} \frac{1}{\sqrt{2\pi\sigma_i^2}} \exp \frac{-(x_i - \mu_i)^2}{2\sigma_i^2}$$
$$= \frac{1}{2} [t \ln 2\pi + \sum_{i=1}^{t} \ln \sigma_i^2 + \sum_{i=1}^{t} \frac{(x_i - y_i')^2}{2\sigma_i'^2}].$$
(31)

Table 2 reports our experimental results. Furthermore, statistic at significance analysis is summarized in Table 3. Since the distribution of NLLs is difficult to solve, we conduct paired one-tailed t-tests to investigate the improvement of using the SAVL 'G model against other benchmark methods. The tests only require the differences to be roughly cormally distributed, which is justified by the Shapiro-Wilk's W for all the pairs. Though we still list results of the Wilcoxon signed-rank test for reference.

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Our null hypothesis is that the average performance of \dots SAVING model among different stocks is identical to or worse than the performance of the benchmark method. The hypothesis is rejected for VRNN, NSVM, LSTM and s+LSTM \dots a significance level of 0.05 and for GARCH and GP-vol at a significance level of 0.' N sufficient evidence suggest that the SAV-ING model performs better than modified GARCH ariants, though the relatively small p-values

still encourage to prefer the SAVING model cite. FG. RCH, TARCH, and GJR-GARCH.

Table 3: Pairwise statistical analysis of the perform. The SAVING model against other benchmarks, measured by NLLs.

Statistic	GARCH [4]	EGARCH [18]	AKC. "34]	GJR [19]	GP-vol [35]	VRNN [7]	NSVM [8]	LSTM [21]	s+LSTM
Shapiro-Wilk's W	0.96	0.96	0.95	0.95	0.96	0.98	0.97	0.90	0.92
p-value	0.78	0.82	<u>`70</u>	0.66	0.76	0.96	0.91	0.22	0.37
paired one-tailed t	1.42	1.33	1.28	1.25	1.51	2.15	2.86	40.44	6.43
p-value	0.09*	0.11).12	0.12	0.08*	0.03**	0.01**	0.00**	0.00**
Wilcoxon's W	14.0	15.0	15.0	15.0	12.0	8.0	5.0	0.0	0.0
p-value	0.17	0.20	0.2	0.20	0.11	0.05**	0.02**	0.01**	0.01**

The SAVING model outpel forms other compared methods on 8 out of 10 stocks in terms of NLL. We compare as erministic linear models and deep neural models. Unlike previous studies, we do not filled ap neural models, such as VRNN and NSVM to be superior to linear models. This may due to the use of different datasets and the difficulty of model tuning. In fact, all the linear model variants exhibit similar and stable behavior, though GJR-GARCH and TARCH perfor. slightly oetter than EGARCH and follows the original GARCH. It is worth mentioning that the TU-GARCH model even produces better results on two stocks and also obtained very similing rough the stocks. This observation justifies the necessity of considering symmetric shock for volatility modeling.

LST^M and ...LSTM show very different results because these two models actually forecast only r arns, it is a great amount of information is lost. The volatility is later derived using a naïve variance estimation based on both observed and forecasted values. Furthermore, the way to incorporate sentiment time series is by simple concatenation. While experiments of the SA TNC model suggest this configuration of simple concatenation is not favored because we need t simultaneously minimize error for sentiment prediction. In some extreme cases (2 out



Figure 5: Return and sentiment series of TSLA. (Colors can be better displaye in the web version of this article.)



Figure 6: Forecasted volatility of TSL , by + o models. (Colors can be better displayed in the web version of this article)

of 10), introducing sentir . ht increases the error of predictions. This not only happens to the LSTM/s+LSTM pair but also the SAVING/VRNN pair. Despite these rare cases, incorporating sentiment still signific and improves LSTM based naïve volatility forecasting, reducing average NLL by 0.6936.

The SAVING mode, on the other hand, takes advantage of both sentiment information and the expressive p wer of a VRNN. Figure 5 shows the log returns of TSLA, where sentiment time series are called to at into the chart. Although some movement segments are seemingly aligned, this completed to at relation between sentiment and asset prices is hard to capture with linear models. Figure 6 provides forecasted volatility of the SAVING model and a GARCH model. We observe that the SAVING model can swiftly adapt to the current fluctuation level whereas CARCL suffers from a long recovery time from previous shocks, consistent with [8]. For this reason, the SAVING forecasting exhibits some desired properties, e.g., stationary, so

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that many finar cial models assuming a latent volatility still apply. The forecasting also shows pseudo-cycrical fluctuation, which is the case for returns as markets close regularly on weekends and 'voli rays.

The recent peak on day 358 (August 7, 2018) corresponds to the drastic juip after Elon Musk announced his take-private plan on Twitter. We observe that the price chickly fell back in the following days after the news sentiment faded away. It is arguable that in a elatively long term the stock's volatility has really been influenced. However, the GARCh forecasting, based on the observed results from day 240 to day 290, seems to need montias of digest this shock without considering market sentiment (see Figure 6).

6. Related Work

Volatility is a fundamental concept which many financial applications ouild on, such as asset/derivative pricing, hedging, and portfolio optimization [11, 381]. A group of deterministic linear models [4, 18, 19] pioneered time-varying volatility 1 or ding. However, these models can be disputed by noise-contaminated data, which is unifortunate1; common in the financial world. Stochastic models, e.g., [39, 35] are thus developed to nuise this weakness. In studies of computational intelligence, fuzzy logic and fuzzy time peries are also widely used to to model time-varying volatility [40, 41].

Recent developments of RNN provided us the possibility of analyzing time series with models having usually hundreds or thousands times of parometers than classical models. Specifically, VRNN models that encode variance with model variable. [7, 8] are suitable for volatility modeling. Other approaches, such as reinforcement 'ear' m_b, are explored to implicitly model risk aversion from simulated portfolio performance [4.]. These models are powerful but pure data

mining on past observations.

Since the relation between market sentime t and price movement has been widely testified [14, 15, 9], it would be more mean. The seek for additional predictive power by incorporating this external information. More buildly speaking, the community witnessed a trend of grounding knowledge to connection introduction buildly speaking, the community witnessed a trend of grounding knowledge to connection in the models in recent years, thanks to the progress in text mining [43], text categorization [4], and text clustering [45] techniques. For instance, Ding et al. [10] extracted events from here's and incorporated event embedding vectors into a deep convolutional neural network (*DCNN*) for stock price prediction; Luo et al. [46] incorporated manually-designed query-driften *e* and in to employ expert knowledge for RNN-based financial sentiment analysis; Xing et al. [17] used the business classification knowledge to model stock relationships with applice on to portfolio construction. We believe this idea can produce more fruitful results in many scenary.

7. Conclusion

In this work, we p oposed the SAVING model to incorporate market sentiment as a form of external knowled are or v fatility forecasting. The model inherits the expressive power of deep VRNNs, and further a fore effective ways to align data from two different sources. The generalized model not only provides an interface to external knowledge bases but also captures the bi-direction. I interaction between market sentiment and asset price movements. Experiments show that the GLARCH, GP-vol, VRNN, and NSVM. Future work includes quantification and visualization of sentiment-volatility interaction. We also plan to leverage sentiment knowledge bases of asset returns of unstribution agnostic models.

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