




SemGloVe: Semantic Co-Occurrences for GloVe From BERT

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Abstract—GloVe learns word embeddings by leveraging statistical information from word co-occurrence matrices. However, word pairs in the matrices are extracted from a predefined local context window, which might lead to limited word pairs and potentially semantic irrelevant word pairs. In this paper, we propose *SemGloVe*, which distills *semantic co-occurrences* from BERT into static GloVe word embeddings. Particularly, we propose two models to extract co-occurrence statistics based on either the masked language model or the multi-head attention weights of BERT. Our methods can extract word pairs limited by the local window assumption, and can define the co-occurrence weights by directly considering the semantic distance between word pairs. Experiments on several word similarity datasets and external tasks show that SemGloVe can outperform GloVe.

Index Terms—Word representations, contextual word embeddings, self-attention network, pre-trained language models.

I. INTRODUCTION

WORD embeddings [1], [2], [3] represent words with low-dimensional real-valued vectors. They can be useful for lexical semantics tasks, such as word similarity and word analogy, and downstream natural language processing (NLP) tasks [4], [5], [6], [7]. Most existing methods use local window-based methods [2], [3], [8] or matrix factorization of global statistics [9] to learn syntax and semantic information from large-scale corpus. In this paper, we investigate GloVe in details.

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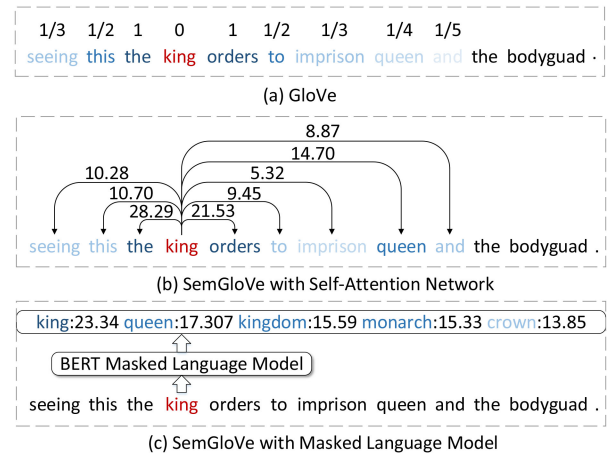


Fig. 1. GloVe (a) and Our two proposed models (b) and (c). The target word and the context word are in red and blue colors, respectively. In (a), the numbers are relevance score, which are position-based distance. In (b) and (c), the relevance scores are the self-attention weights, and the logits of the language model, respectively.

GloVe [9] combines matrix factorization methods with local window context, generating word embeddings by leveraging statistical information from a global word-word co-occurrence matrix. Word-word pairs in the matrix are extracted from a predefined local context window, and the relevance is measured by a position-based distance function. For example, as shown in Fig. 1(a), when targeting at the word “king” with the five-words context window, the word pair “king-queen” can be extracted with a co-occurrence score 1/4, since “queen” is four words away from “king”. However, this co-occurrence matrix generation procedure can suffer from two potential problems. First, the counting word pairs are limited by the local context window. Second, the heuristic weighting function does not measure the relevance score directly regarding to the semantic similarities between word pairs, leading to inaccurate co-occurrence counts. For example, “king” and “orders” are weakly correlated in the sentence “he orders a copy of the king of fighters”.

One potential solution to the above problems is BERT [10], which is a pre-trained language model based on deep bidirectional Transformers [11]. Previous work has shown that the contextualized representations produced by BERT capture morphological [12], [13], lexical [12], syntactic [14], [15] and semantic knowledge [16], [17]. These knowledge can be disentangled using knowledge distillation models [18], [19] or variational

inference [14]. Inspired by these research ideas, we hypothesize that the word-word co-occurrence matrix can be distilled from BERT.

We name the co-occurrences distilled from BERT as *semantic co-occurrences*, thus proposing *SemGloVe* to improve GloVe. Our proposed method can distill contextualized semantic information from BERT into static word embeddings. In particular, we present two models. As shown in Fig. 1(b), the first model is based on self-attention networks of BERT (SAN; Section III-A). The idea is to use attention values in SAN for semantic co-occurrence counts. Intuitively, the SAN model can solve the second issue of GloVe by using the self-attention weights as the word pair scoring function. For example, the relevance score of the “king-queen” pair in Fig. 1(b) is 14.7, which is much larger than the 9.45 score of the “king-to” pair even though “to” is closer to “king” than “queen” is.

As shown in Fig. 1(c), the second is based on the masked language model (MLM; Section III-B) of BERT. The idea is to distill word probabilities from a masked language model for co-occurrence counts. First, it generates word pairs by masking the target word to predict context words from the whole vocabulary, which can avoid the local context window restriction of GloVe. The output context words and the target word can be regarded as co-occurring word pairs. For example, in Fig. 1(c), after masking “king,” BERT outputs context words such as “queen” and “crown”. Both “king-queen” and “king-crown” are regarded as valid co-occurrences even though “crown” does not appear in this sentence. Compared with the local window context, we hypothesize that the distributional hypothesis [20] works better for the masked language model, because words that occur in the same output contexts tend to have similar meanings. Second, the MLM model uses the logits of output words from BERT as the word pair scoring function, which can solve the first problem of GloVe.

Experiments on word similarity datasets show that SemGloVe can outperform GloVe. We also evaluate SemGloVe on external Chunking, Part-Of-Speech (POS) tagging and named entity recognition (NER) tasks, again showing the effectiveness of SemGloVe. Specifically, our analysis shows that SemGloVe has two advantages: 1) it can find semantic relevant word pairs which cannot be captured by GloVe; 2) SemGloVe can generate more accurate global word-word co-occurrence counts compared to GloVe.

SemGloVe gives better averaged results compared with existing state-of-the-art (non-contextualized) embedding methods on both intrinsic and extrinsic evaluation tasks. In addition to its theoretical interest, this leads to three contributions to the research community. First, it enriches the toolbox for computational linguistics research involving word representations that do not vary by the sentence, such as lexical semantics tasks. Second, it adds to the set of input embeddings that are orders of magnitudes faster compared with contextualized embeddings as it only requires training one time and then can be efficiently used for many downstream tasks. Third, SemGloVe provides better static word vectors, which have been shown to be supplementary to contextual word embeddings for downstream tasks, such as text classification task [21] and named entity recognition

task [22]. Our code and SemGloVe embeddings are available at <https://github.com/leileigan/SemGloVe>.

II. BACKGROUND

In this section, we briefly review GloVe and BERT, which our models are based on.

A. Glove

Given a training corpus, GloVe first obtains the global word-word co-occurrence counts matrix \mathbf{X} , whose entries X_{ij} represents the total number of times word $w_j \in V$ occurring in the context of word $w_i \in V$, where V is the word vocabulary of the training corpus. Formally, let $\mathbb{C}(w_i)$ be the set of the local window context of each w_i in the training corpus. GloVe defines X_{ij} with regards to the **position-based distance** between w_i and w_j as:

$$X_{ij} = \sum_{C_k(w_i) \in \mathbb{C}(w_i)} \sum_{w_j \in C_k(w_i)} \text{dis}(w_i, w_j) \quad (1)$$

$$= \sum_{C_k(w_i) \in \mathbb{C}(w_i)} \sum_{w_j \in C_k(w_i)} \frac{1}{|p_j - p_i|}, \quad (2)$$

where $C_k(w_i)$ is a local window context of w_i , p_j and p_i are the positions of w_j and w_i in the context, respectively. Intuitively, words closer to w_i receive larger weights.

Denote the embedding of a target word w_i and the context embedding of a context word w_j as e_i and e'_j , respectively. GloVe learns the word vectors by optimizing the following loss function:

$$J = \sum_{i=1}^V \sum_{j=1}^V f(X_{ij}) (e_i^T e'_j + b_i + b'_j - \log X_{ij})^2, \quad (3)$$

where b_i and b_j represent biases for w_i and w_j respectively, and $f(\cdot)$ is a weighting function. $f(\cdot)$ assigns lower weights to less frequent co-occurrences:

$$f(X_{ij}) = \begin{cases} (X_{ij}/x_{\max})^\alpha & \text{if } X_{ij} < x_{\max}, \\ 1 & \text{otherwise,} \end{cases} \quad (4)$$

where x_{\max} and α are hyper-parameters.

After training with optimization methods, $e_i + e'_i$ is taken as the final word embeddings for w_i .

B. Bert

BERT is trained from large scale raw texts using masked language modeling task (MLM) with a deep bidirectional Transformer, which consists of multiple self-attention encoder (SAN) layers. Specifically, MLM masks a certain token as a special symbol $\langle \text{MASK} \rangle$ (or a random token) randomly, and predicts the masked token using the contextualized output of the topmost layer.

Formally, given a token sequence $W = \{w_1, w_2, \dots, w_n\}$, a certain token w_i ($i \in [1..n]$) is masked. The input layer \mathbf{H}^0 and

each intermediate layer representation \mathbf{H}^j are defined as:

$$\begin{aligned} \mathbf{H}^0 &= [e_1; \dots; e_{i-1}; e_i; e_{i+1}; \dots; e_n] + \mathbf{W}_p \\ \mathbf{H}^j &= \text{SAN_Encoder}(\mathbf{H}^{j-1}) \quad j \in [1 \dots K], \end{aligned} \quad (5)$$

where e_i is the embedding of w_i , \mathbf{W}_p is the position embedding matrix, **SAN_Encoder** is SAN based encoder and K denotes the number of SAN layers. More details about **SAN_ENCODER** can be found in [11]. For MLM, BERT predicts w_i using

$$\text{logits}(\mathbf{h}_i^K) = \mathbf{W}\mathbf{h}_i^K \quad (6)$$

$$\mathbf{p}[w_i] = \text{softmax}(\text{logits}(\mathbf{h}_i^K)) \quad (7)$$

where \mathbf{W} is a model parameter and $\mathbf{p}[w_i]$ denotes $P(w_i|w_1, \dots, w_{i-1}, \langle \text{MASK} \rangle, w_{i+1}, \dots, w_n)$.

Given a set of unlabelled text, $D = \{W^i\}_{i=1}^N$, BERT is trained by maximizing the following objective function:

$$J = \sum_{i=1}^N \sum_{j=1}^{|W_i|} \mathbf{P}[w_i^j]. \quad (8)$$

III. SEMANTIC GLOVE

We replace the hard counts of co-occurrences into real values from BERT, according to self-attention scores and MLM probabilities, respectively.

A. Semantic Co-Occurrences From Multi-Head Self-Attention

In this section, we leverage the multi-head self-attention weights of BERT to measure the semantic relationships of tokens instead of the heuristic position-based distance function of GloVe.

Specifically, given a sentence $W = \{w_1, \dots, w_K\}$ from the training corpus, a window size S and a pre-trained BERT model, we wish to define the word-to-word semantic distance (i.e., the *dis* function in Equation (2)) using the self-attention weights of BERT. Since BERT uses word pieces or byte-pair encodings (BPE; [23]) to segment words into BPE tokens, we firstly convert the original BPE-to-BPE attention weights to word-to-word attention weights.

Let the corresponding BPE token sequence is $T = \{t_1, \dots, t_L\}$, N and M be the number of layers and heads of the BERT model, and $\mathbf{AT}_{ij} \in \mathbb{R}^{L \times L}$ be the BPE token attention weights matrix of the j -th head in the i -th layer. We sum all heads and layers attention weights into one BPE-to-BPE attention weight matrix as follows:

$$\mathbf{AT} = \sum_{i=1}^N \sum_{j=1}^M \mathbf{AT}_{ij}. \quad (9)$$

where $\mathbf{AT} \in \mathbb{R}^{L \times L}$ is the averaged token-to-token attention weight matrix.

Then, we generate the word-to-word attention weight matrix $\mathbf{AW} \in \mathbb{R}^{K \times K}$ by averaging the BPE-to-BPE attention weights. For w_j within the local window context of word w_i , $j \in [i - S, i + S] \cap j \neq i$, we denote the attention weight (a real value)

from word w_i to w_j as \mathbf{AW}_{ij} following:

$$\mathbf{AW}_{ij} = \frac{1}{m \times n} \sum_{k=s_1}^{s_m} \sum_{l=t_1}^{t_n} \mathbf{AT}(k, l), \quad (10)$$

where $\mathbf{AT}(k, l)$ is the attention weight from BPE token t_k to t_l , m and n are the number of subwords of w_i and w_j , respectively. To remove semantic irrelevant words, we sort \mathbf{AW}_{ij} in descending order, and select the top- S words as w_i 's context words $C(w_i)$.

For now, values in \mathbf{AW} are still raw attention weights extracted from a pre-trained model, which are unnormalized and are not appropriate for training GloVe. To normalize the distance between the target word w_i and the context word w_j within 0 and 1, the following *Division* distance function is introduced:

$$\text{dis}_{sa}(w_i, w_j) = \mathbf{AW}_{ij} / \mathbf{AW}_{i1}. \quad (11)$$

Finally, for the whole corpus, elements in the global word-to-word co-occurrence count matrix \mathbf{X} is accumulated as:

$$X_{ij} = \sum_{C_k(w_i) \in \mathbb{C}(w_i)} \sum_{w_j \in C_k(w_i)} \text{dis}_{sa}(w_i, w_j). \quad (12)$$

where $C_k(w_i)$ is the context words of w_i defined by the multi-head self-attention weights, and $\mathbb{C}(w_i)$ is the set of each w_i 's context in the training corpus.

We name the GloVe model training on this semantic word-to-word co-occurrence counts as SemGloVe_{sd} .

B. Semantic Co-Occurrences From Masked Language Model

BERT pre-trained using deep bidirectional Transformers with the MLM task provides a dynamic way to define context for target word, which can avoid semantic irrelevant word pairs from a local window context. In this section, we introduce another method to distill semantic word-word co-occurrence counts by leveraging the MLM task of BERT.

Formally, given a sentence $W = \{w_1, \dots, w_K\}$ from the training corpus, the corresponding BPE token sequence $T = \{t_1, \dots, t_L\}$, a window size S and the topmost layer output \mathbf{h}_i^K of the **SAN_Encoder**, we define the context tokens $\mathcal{C}(w_i)$ as the output tokens of the MLM of BERT, and calculate the word-to-word semantic distance (i.e., the *dis* in Equation (2)) using the logits in Equation (6).

Specifically, we first generate the BPE-to-BPE co-occurrence matrix $\mathbf{M} \in \mathbb{R}^{L \times L}$ to deal with the same BPE problem in Section III-A. To be more specific, we feed the original BPE token sequence T into the MLM model and sort the obtained output tokens in descending order with respect to $\text{logits}(\mathbf{h}_i^K)$, and then select the top $2S$ tokens to constitute t_i 's context tokens, denoted as $\mathcal{C}(t_i) = \{t_i^{(1)}, t_i^{(2)}, \dots, t_i^{(2S)}\}$. The corresponding logits are denoted as $G(t_i) = \{g_i^{(1)}, g_i^{(2)}, \dots, g_i^{(2S)}\}$. It is worth noting that token t_i actually is not masked. In preliminary experiments, we did try to mask t_i in the input sentence, however, this strategy did not give a better result. We hypothesize that the information carried by t_i is useful to predict the most similar co-occurring words. If masking t_i , more noisy word pairs will be introduced.

Similar in Section III-A, the distance between the target token t_i and the context token $t_i^{(j)}$ is calculated as:

$$\text{dis}_{mlm}(t_i, t_i^{(j)}) = g_i^{(j)} / g_i^{(1)}. \quad (13)$$

Then, for the whole corpus, elements in the global BPE-to-BPE co-occurrence matrix \mathbf{M} is calculated as:

$$M_{ij} = \sum_{C_k(t_i) \in \mathbb{C}(t_i)} \sum_{t_j \in C_k(t_i)} \text{dis}_{mlm}(t_i, t_j). \quad (14)$$

where $C_k(t_i)$ is the context of t_i defined by the masked language model, and $\mathbb{C}(t_i)$ is the set of each t_i 's context in the training corpus.

Finally, we generate the global word-to-word co-occurrence matrix by averaging the BPE-to-BPE matrix as:

$$X_{ij} = \frac{1}{m \times n} \sum_{k=s_1}^{s_m} \sum_{l=t_1}^{t_n} M_{kl}, \quad (15)$$

where m and n are the number of subwords of w_i and w_j , respectively. Similar ideas can be found in [24], [25] that leverages MLM to construct synonym dictionary.

The GloVe model trained on this kind semantic co-occurrences is named as SemGloVe_{md}.

IV. EXPERIMENTS

We compare SemGloVe with GloVe on a range of intrinsic and extrinsic evaluation tasks, discussing the role the semantic co-occurrence plays in the training process.

A. Settings

To give fair comparisons with previous methods, we follow [26] to use the Wikipedia¹ dump corpus as our training dataset, which is processed to only keep words appearing more than five times. The dataset consists of 57 million sentences and 1.1 billion tokens.

For all our experiments, we set $x_{\max} = 10$, $\alpha = 0.75$, the vectors dimension to 300, the window size S to 5, and the number of iteration to 100. AdaGrad [27] is used as the optimizer with initial learning rate $lr = 0.05$. We dump the weights using the uncased BERT-large model with whole word masking, which has 24 layers and 12 attention heads². The code is implemented by PyTorch and MindSpore.

B. Baselines and Evaluation Methods

In addition to GloVe, we also compare SemGloVe with other state-of-the-art embedding methods, including Word2Vec [3], Deps [28], Fasttext [8], SynGCN and SemGCN [26], on several intrinsic and extrinsic semantic evaluation tasks. In addition to the GloVe baseline under the same settings, we also download GloVe_{6B} from the official website as one baseline, which is trained on 6 billion tokens³ and contains five times more tokens than the Wikipedia dump we used.

We evaluate the intrinsic task on word similarity datasets, including WordSim-353 [29], and SimLex-999 [30]. Spearman correlation is taken as the main metric.

For extrinsic evaluation, we build a sentence-state LSTM (S-LSTM) [31] based sequence labeling model which takes the concatenation of ELMo [32] and GloVe or SemGloVe as inputs. S-LSTM is a variant of LSTM, which parallelly updates the states of words by exchanging information locally and globally. The number of parameters of S-LSTM is 29.8 M. We compare this method with BERT_{base} which has 110 M parameters on a range of tasks, including Chunking, POS tagging and Named Entity Recognition (NER). The datasets used for evaluation are CoNLL-2000, the Wall Street Journal (WSJ) portion of the Penn Tree Bank (PTB) and CoNLL-2003, respectively.

C. Development Experiments

Development experiments are conducted on the WS353S dataset to compare the performance of GloVe and SemGloVe with different hyper-parameters settings. To be specific, we investigate the influence of vector dimension, corpus size and x_{\max} value on the performance.

1) *Effect of Vector Dimension:* We evaluate GloVe and SemGloVe with different vector dimensions, ranging from 50 to 400. For dimensions smaller than 300, the iteration number is set to 50, otherwise, it is set to 100. As shown in Fig. 2(a), SemGloVe outperforms GloVe under different vector dimension settings. When increasing the vector size from 50 to 300, both GloVe and SemGloVe can improve the performance on the WS353S dataset. However, when further increasing the vector size to 400, GloVe has a slight decrease in performance while SemGloVe_{md} can keep the results stable. For a fair comparison, we choose 300 as the final vector size.

2) *Effect of Corpus Size:* To investigate the influence of corpus size, we divide the whole training corpus into 8 parts. GloVe and SemGloVe are trained on 1/8, 2/8, 4/8, 6/8 and 8/8 corpus parts, respectively. According to the corpus size, x_{\max} is set to 1.25, 2.5, 5, 7.5 and 10, respectively. As shown in Fig. 2(b), SemGloVe outperforms GloVe in all corpus size settings. As the corpus size increases, GloVe and SemGloVe_{sd} obtain better performance. In the meantime, SemGloVe_{md} can achieve reasonable results even with a small corpus size. We suppose that SemGloVe_{md} can capture sufficient word-word co-occurrences counts under small corpus size, which we will analyze in Section IV-E.

3) *Effect of x_{\max} Value:* To evaluate the effect of x_{\max} , we train our models with different x_{\max} values. As shown in Fig. 2(c), SemGloVe outperforms GloVe under different x_{\max} values. GloVe and SemGloVe_{sd} achieve the best results when x_{\max} is set to 10, while SemGloVe_{md} maintains strong and stable results with different x_{\max} values. The reasons we suppose can be explained as follows. As indicated by Equation 3 and 4, co-occurrences with frequencies smaller than x_{\max} will be assigned lower weights for training, thus for window based contexts which are not able to capture high-quality co-occurrences, the choice of x_{\max} is important for the final performance. A large x_{\max} value will lead to the neglect of useful word-word

¹<https://dumps.wikimedia.org/enwiki/20180301>

²<https://github.com/google-research/bert>

³<https://nlp.stanford.edu/projects/glove/>

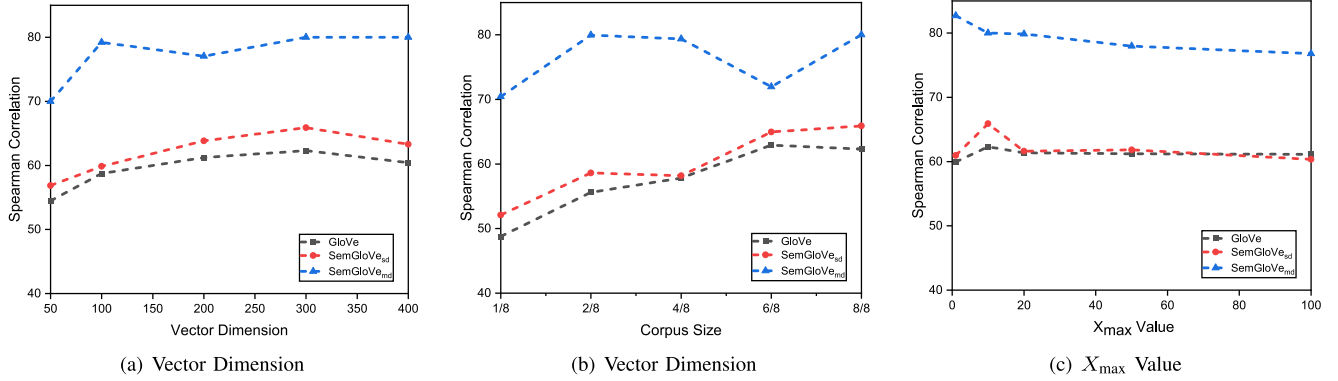


Fig. 2. Performance on WS353S dataset as function of vector dimension, corpus size and x_{\max} value. (a) Vector Dimension (b) Vector Dimension (c) X_{\max} Value.

TABLE I

INTRINSIC EVALUATION: COMPARISON ON WORDSIM-353 (WS353) AND SIMLEX-999 (SIMLEX999) DATASETS. WS353S AND WS353R ARE SUBSETS OF WORDSIM-353, WHICH ARE USED TO MEASURE THE RELATEDNESS AND SIMILARITY OF WORDS, RESPECTIVELY

Models	WS353	WS353S	WS353R	SimLex999	Average
Word2Vec	61.6	69.2	54.6	35.1	52.6
Deps	60.6	65.7	36.2	39.6	50.5
Fasttext	68.3	74.4	65.4	34.9	60.8
SemGCN	60.9	65.9	60.3	48.8	59.0
SynGCN	60.9	73.2	45.7	45.5	56.3
GloVe	52.6	62.3	55.5	28.2	49.7
GloVe _{6B}	56.5	64.6	50.0	31.3	50.6
SemGloVe _{sd}	56.0	65.9	56.3	31.9	52.5
SemGloVe _{md}	69.7	80.0	68.9	46.5	66.3

The bold results are the best results.

co-occurrences, while a small value will bring more noises. However, for SemGloVe_{md} which captures context from deep bidirectional Transformers, there exists less noisy co-occurrences. As a result, the performance can maintain stable with different x_{\max} values. We set x_{\max} to 10 in the remaining experiments.

D. Final Results

1) *Intrinsic Evaluation Results*: The final intrinsic evaluation results of SemGloVe and the baselines are listed in Table I. First, we find that SemGloVe_{sd} and SemGloVe_{md} outperform GloVe on the four word similarity evaluation datasets. Specifically, SemGloVe_{sd} obtains 5.6% absolute increase in performance on average, which demonstrates that self-attention weights of BERT are better to measure word similarities than the original position-based distance method. In addition, compared with GloVe, SemGloVe_{md} gives 33.4% absolute increase in performance on average, which demonstrates that masked language model of BERT can model the context of words better than the predefined local window context, and produce more semantic relevant word pairs. Moreover, We also find that the averaged results of SemGloVe_{md} outperform all the best methods in the literature.

TABLE II

EXTRINSIC EVALUATION: COMPARISONS ON CHUNKING, POS TAGGING AND NER TASKS ON CONLL-2000, THE WALL STREET JOURNAL (WSJ) PORTION OF THE PENN TREE BANK (PTB) AND CONLL-2003. THE METRICS FOR THE THREE TASKS ARE F1-VALUE, ACCURACY AND F1-VALUE, RESPECTIVELY

Models	Chunking	POS	NER	Average
BERT _{base}	96.60	97.77	92.40	95.59
GloVe	96.72	97.65	92.27	95.21
SemGloVe	96.75	97.70	92.60	95.68

The bold results are the best results.

Since SemGloVe_{md} performs better than SemGloVe_{sd} on intrinsic tasks, we take them as the final SemGloVe.

2) *Extrinsic Evaluation Results*: The final extrinsic evaluation results are shown in Table II. We find that SemGloVe outperforms GloVe on three tasks, which demonstrates that SemGloVe contains more semantic information for downstream tasks. Specifically, SemGloVe gives 0.47% absolute increase in performance on average, respectively. Furthermore, compared with contextual word representations BERT_{base}, SemGloVe also shows competitive performance.

The comparisons on extrinsic tasks is to show that SemGloVe (static word vectors) is still useful for downstream tasks, instead

TABLE III
SOME SPECIFIC WORD-WORD CO-OCCURRENCE COUNTS OF GLOVE AND SEMGLOVE

Methods	GloVe	SemGloVe _{sd}	SemGloVe _{md}
$\langle \text{cat, cats} \rangle$	0.33×10^2	0.86×10^2	3.48×10^4
$\langle \text{paris, french} \rangle$	8.23×10^2	1.41×10^3	5.21×10^4
$\langle \text{man, woman} \rangle$	1.48×10^3	2.57×10^3	1.25×10^5
$\langle \text{himself, oneself} \rangle$	0	0	4.42×10^4
$\langle \text{meanwhile, meantime} \rangle$	0	0	2.72×10^4
$\langle \text{additionally, moreover} \rangle$	0	0	2.90×10^4
$\langle \text{biophysical, biochemical} \rangle$	12.53	12.93	1.16×10^2
$\langle \text{egyptologist, archaeologist} \rangle$	15.00	17.30	0.39×10^2
$\langle \text{egyptologist, egyptian} \rangle$	11.32	8.89	8.58×10^3

of showing the weakness of contextualized embeddings as input representations. Another advantage of GloVe and SemGloVe, as compared with BERT, is that they are light weight and much faster for training and testing for downstream tasks.

E. Analysis

We give analysis to the generated word-word co-occurrence counts of GloVe and SemGloVe, and try to answer the following research questions: (1) Can SAN weights of BERT be used to measure semantic similarity between word pairs, and lead to more accurate co-occurrence counts? (2) Can masked language model of BERT generate more semantic relevant word pairs? (3) Can the proposed *Division* distance function be better than the original position-based distance function?

Co-occurrence Counts Analysis: To answer above questions, we analyze the difference of co-occurrence counts between GloVe and SemGloVe from two aspects, some specific word pairs and the general statistical information. First, we investigate some representative co-occurrence counts. As shown in Table III, word pairs of the first three rows, which are close in semantic, such as $\langle \text{paris, french} \rangle$, can be found in all five methods. However, SemGloVe_{sd} can generate larger co-occurrence counts compared with GloVe, which proves that self-attention weights of BERT can assign larger counts to more semantic similar word pairs within the context. In fact, SemGloVe_{md} can reach an average of 50 times counts of GloVe or SemGloVe_{sd}. We suppose that the words in a window context can be diverse and noisy, and thus distract the total co-occurrence counts. This helps to explain why SemGloVe_{md} trained on small size corpus can still achieve strong performance. Furthermore, SemGloVe_{md} can generate semantic relevant word pairs in the second three rows, which cannot be found in GloVe or SemGloVe_{sd}. This is because the two methods generate word pairs from a local window, while SemGloVe_{md} can output most similar words over the whole vocabulary based on a deep bidirectional context.

As shown in Equation 14 and Equation 15, SemGloVe_{md} firstly calculate the BPE-to-BPE co-occurrence count and then generate the word-to-word co-occurrence matrix by averaging the counts of the subword pairs. We hypothesize this design can lead to rich semantic word pairs of SemGloVe_{md} because word pairs with common subwords will be connected and obtain

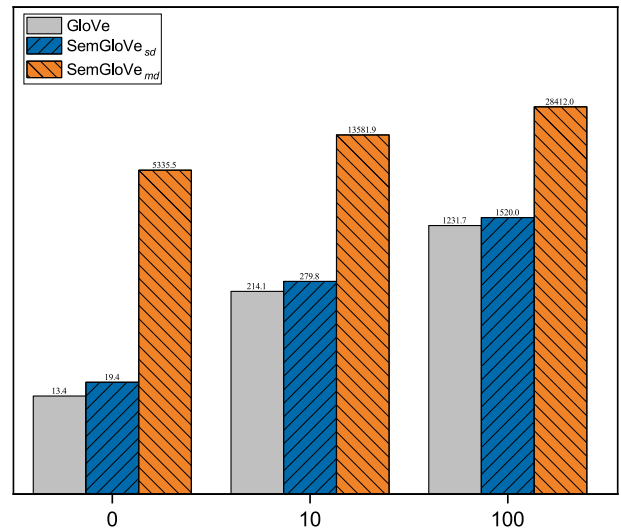


Fig. 3. Average word-word co-occurrence counts of GloVe and two variants of SemGloVe.

a large co-occurrence count. We give some examples in the third three rows of Table III. For instance, word “egyptologist” consists of two subwords “Egypt” and “##ologist,” which lead to rich semantic word pairs, $\langle \text{egyptologist, egyptian} \rangle$ and $\langle \text{egyptologist, archaeologist} \rangle$, respectively.

Second, we explore the average word-to-word co-occurrence counts of GloVe and SemGloVe by dividing the counts into three groups. The minimum counts of the first, second and third groups are 0, 10, 100, respectively. The average count of each group is equal to the total counts divided by the number of word pairs. As shown in Fig. 3, the average counts of SemGloVe_{sd} are larger than GloVe in all groups. In addition, the average counts of SemGloVe_{md} surpass the number of GloVe and GloVe_{sd} by a large amount in all three groups. This again shows that the SAN weights of BERT can help to determine the semantic distance between words, while MLM can generate semantic relevant word pairs without limiting by the local window context.

Effect of Distance Functions: Different from the position-based distance function of GloVe, our *Division* distance function is based on either the weights of SAN or the output logits of MLM. To investigate whether our distance function captures

TABLE IV
COMPARISONS OF DIFFERENT DISTANCE FUNCTION

Models	WS353	WS353S	WS353R	SimLex999	Average
GloVe	52.6	62.3	55.5	28.2	49.7
SemGloVe _{sr}	54.0	62.8	54.9	29.3	50.3
SemGloVe _{sd}	56.0	65.9	56.3	31.9	52.5
SemGloVe _{mr}	67.8	79.2	66.7	45.1	64.7
SemGloVe _{md}	69.7	80.0	68.9	46.5	66.3

The bold results are the best results.

TABLE V
ANALYSIS OF WINDOW SIZE. THE NUMBERS IN THE PARENTHESES ARE THE TOTAL WORD PAIRS

Models	WS353	WS353S	WS353R	SimLex999	Average
GloVe(0.3B)	52.6	62.3	55.5	28.2	49.7
SemGloVe _{sd} (0.2B)	56.0	65.9	56.3	31.9	52.6
SemGloVe _{sd10} (0.3B)	55.3	63.2	56.4	28.6	50.9
SemGloVe _{sdR} (0.2B)	52.7	60.5	54.6	27.7	48.9
SemGloVe _{md5}	66.1	78.6	67.0	45.3	64.3
SemGloVe _{md}	69.7	80.0	68.9	46.5	66.3

The bold results are the best results.

more semantic knowledge, we first sort the context words according to their SAN weights or MLM logits in descending order, and then directly replace the *Division* function of SemGloVe with position-based distance function, and name the two corresponding method as SemGloVe_{sr} and SemGloVe_{mr}. The comparisons are listed in Table IV. We can observe that the *Division* distance function performs better than the original distance function of GloVe in mapping BERT’s weights into co-occurrence counts, which can be because that the *Division* function leverage information of weights better than the original function.

Effect of Window Sizes: Although SemGloVe with SAN and GloVe have the same window size, the context words in GloVe are twice as many as those in SemGloVe. This is because the context of GloVe is symmetric. In SemGloVe with SAN, in fact, we sort the scores of all the 10 words in descending order, and then select the top 5 words as context words. To analyze the effect of window size, we take ablation studies on the word similarity dataset as shown in Table V. “SemGloVe_{sd10}” is a setting, where we select the top 10 words as context words, while for “SemGloVe_{sdR},” we replace the co-occurrence counts of “SemGloVe_{sd}” with the corresponding counts of GloVe. We can find that the performance of “SemGloVe_{sd10}” is slightly worse than “SemGloVe_{sd},” but still better than GloVe. However, “SemGloVe_{sdR}” reaches almost the same results as GloVe. We conclude that reducing the window size in SemGloVe_{sd} can reserve valuable word pairs.

We also reduce the window size from 10 to 5 in SemGloVe with MLM, and name this setting as SemGloVe_{md5}. As shown in Table V, we can find that reducing the window size in MLM model will decrease the performance.

Effect of Pre-trained Models: Our current SemGloVe is based on BERT-large. To ablate the effectiveness of the proposed

method on different pre-trained language models, we conduct experiments based on ALBERT [33]. The results are listed in Table VI. As been shown, SemGloVe based on ALBERT also gives better results compared with GloVe. We also have tried to train SemGloVe based on RoBERTa [34]. However, RoBERTa is a case-sensitive pre-trained language model and its tokenization is also sensitive to whitespace token. These two characteristics increase the difficulty in calculating the word-to-word counts. As a result, in our experiments, SemGloVe based on RoBERTa did not give competitive results compared with those based on BERT and ALBERT.

Visualization: We use t-SNE [35] to visualize GloVe, SemGloVe_{sd} and SemGloVe_{md} embeddings. As shown in Fig. 4, GloVe has several outliers for classes of city, time, astronomy and politics. One reason is that for outlier words, such as “daybreak,” there are few useful related word pairs in the co-occurrence matrix of GloVe. SemGloVe_{sd} performs better than GloVe, and contains fewer outlier words. However, some classes are not separated clearly. In contrast, SemGloVe_{md} gives the best visualization result among all models. Words from the same class are clustered together, and different classes have clear boundaries. We attribute this to the rich semantic word pairs of SemGloVe_{md}. For the same word “daybreak,” the co-occurrence matrix of SemGloVe_{md} instead contains semantic relevant word pairs, such as < daybreak, today, 1.54×10^3 > and < daybreak, sunday, 3.20×10^3 >.

V. RELATED WORK

1) *Static Word Representations:* Skip-Gram (SG) and Continuous-Bag-of-Words (CBOW) [2], [3] are both local window context based static word vectors, which have been the key components of representation learning and deep learning [36],

TABLE VI
COMPARISONS OF DIFFERENT PRE-TRAINED LANGUAGE MODELS

Models	WS353	WS353S	WS353R	SimLex999	Average
GloVe	52.6	62.3	55.5	28.2	49.7
GloVe _{6B}	56.5	64.6	50.0	31.3	50.6
+BERT-large					
SemGloVe _{md}	69.7	80.0	68.9	46.5	66.3
+ALBERT-large					
SemGloVe _{md}	61.2	72.3	61.4	43.0	59.5

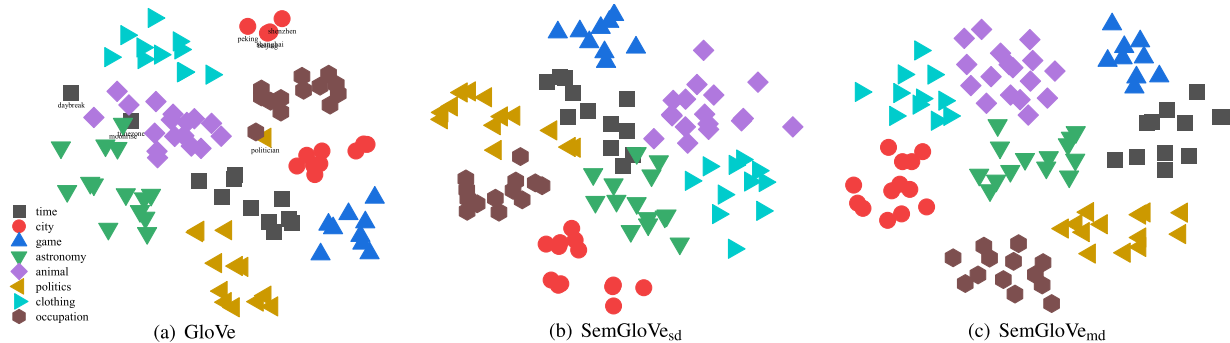


Fig. 4. Visualization of three methods on randomly selected eight classes of words, including time, city, game, astronomy, animal, politics, clothing and creator. Each class contains ten words on average. (a) GloVe (b) SemGloVe_{sd} (c) SemGloVe_{md}.

[37], [38], [39]. The former predicts the context words using the center word, while the latter predicts the center word using its neighbors. [28] improve the word embeddings by injecting syntactic information from the dependency parse trees. FastText [8] enriches word embeddings with subwords. Previous work also investigates how to incorporate external semantic knowledge into the above word embeddings. [40] and [41] propose to post-process word vectors using word synonymy or antonymy knowledge from semantic lexicons or task-specific ontology. [26] leverage graph neural networks to incorporate syntactic and semantic knowledge into word embeddings. [42] jointly train word vectors using a text corpora and a knowledge base, which contains special semantic relations. All these methods inject semantic information from structured data, which is expensive to construct, while our methods can benefit from large-scale language models which are pre-trained on unlabelled corpora.

g) Distilling Knowledge From BERT: [18] introduce knowledge distillation, which can transfer knowledge from a large (teacher) network to a small (student) network. Following this idea, [19] propose to distill knowledge from the last layer of BERT into a single-layer BiLSTM network. [43] propose Patient-KD, which not only learns from the last layer of BERT, but also learns from multiple intermediate layers by two strategies: PKD-last and PKD-skip. TinyBERT [44] learns from the embedding layer, the hidden states and attention matrices of intermediate layers, and the logits output of the prediction layer of BERT. [45] improve sequence to sequence text generation models by leveraging BERT's bidirectional contextual knowledge.

There is also a line of concurrent work trying to derive static vectors for words, phrases and sentences from contextual word embeddings. [46], [47], [48] use the deep contextual hidden representations to improve word2vec [2], [3]. The simplest way to derive static vectors for phrases or sentences is max-pooling or mean-pooling over contextual word embeddings. However, these methods rely on lexical overlaps. To alleviate this issue, [49] obtain phrase-level vectors (Phrase-BERT) from BERT which is fine-tuned with a contrastive objective. [50] derive static vectors for sentences from BERT which is fine-tuned on natural language inference dataset using siamese network structures.

Different from all the previous works, in this paper, we distill semantic knowledge from a pre-trained BERT into GloVe using the weights of SAN and MLM.

VI. CONCLUSION

We present SemGloVe, which replaces the hard counts of GloVe by distilling semantic co-occurrences from BERT. Compared with GloVe, SemGloVe can extract word pairs without local window constraints, and can count co-occurrences by directly considering the semantic distance between word pairs. Intrinsic and extrinsic experiments show that SemGloVe outperforms GloVe.

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